

Exercise 29

In Exercises 29 to 31, use vector methods to describe the given configurations.

The parallelepiped with edges the vectors \mathbf{a} , \mathbf{b} , and \mathbf{c} emanating from the origin

Solution

Assuming that the vectors, \mathbf{a} , \mathbf{b} , and \mathbf{c} , are linearly independent, the entire three-dimensional space is spanned by taking a linear combination of these three.

$$\mathbf{r}(s, t, u) = s\mathbf{a} + t\mathbf{b} + u\mathbf{c}$$

By restricting s , t , and u to be between 0 and 1, only points within the parallelepiped with edge vectors, \mathbf{a} , \mathbf{b} , and \mathbf{c} , are obtained.

$$\{s\mathbf{a} + t\mathbf{b} + u\mathbf{c}, 0 \leq s \leq 1, 0 \leq t \leq 1, 0 \leq u \leq 1\}$$